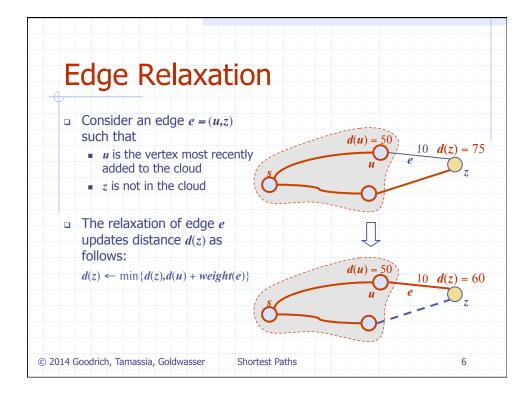
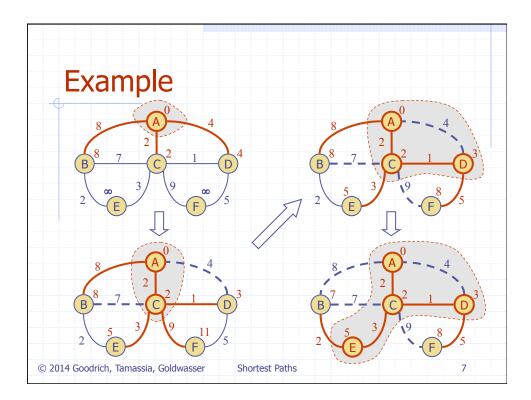
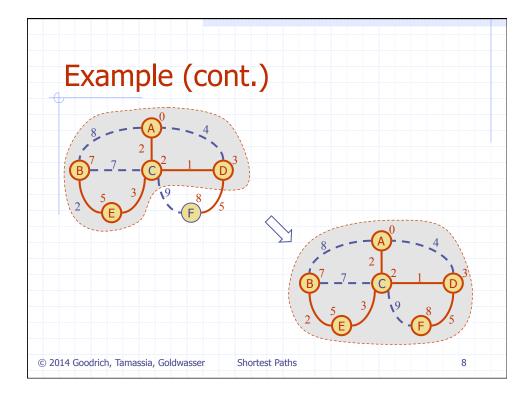
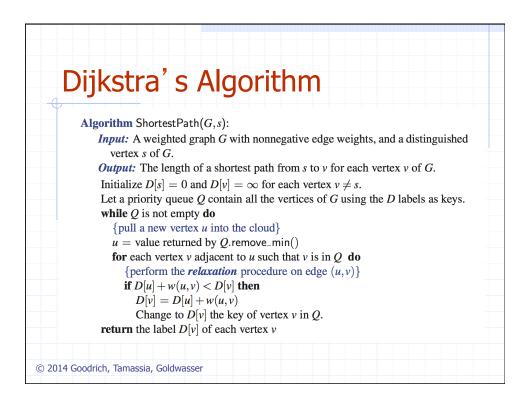


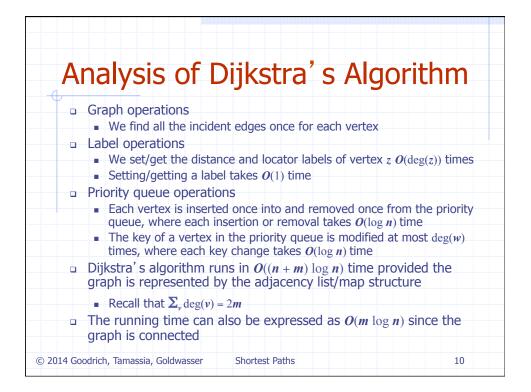
Di	ijkstra' s Algo	ori	thm
	The distance of a vertex v from a vertex s is the length of a shortest path		We grow a "cloud" of vertices, beginning with <i>s</i> and eventually covering all the vertices
	between <i>s</i> and <i>v</i> Dijkstra' s algorithm computes the distances of all the vertices from a given start vertex <i>s</i>		We store with each vertex v a label $d(v)$ representing the distance of v from s in the subgraph consisting of the cloud and its adjacent vertices
	Assumptions: • the graph is connected • the edges are undirected • the edge weights are nonnegative		 At each step We add to the cloud the vertex <i>u</i> outside the cloud with the smallest distance label, <i>d(u)</i> We update the labels of the vertices adjacent to <i>u</i>



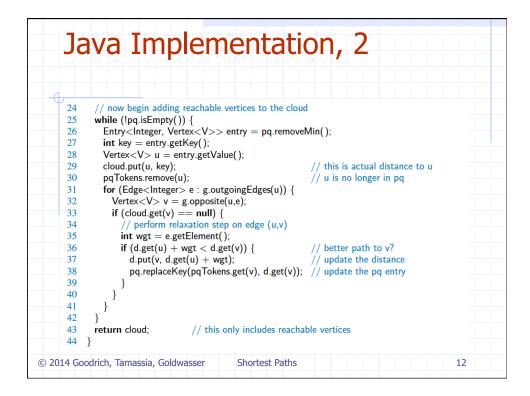


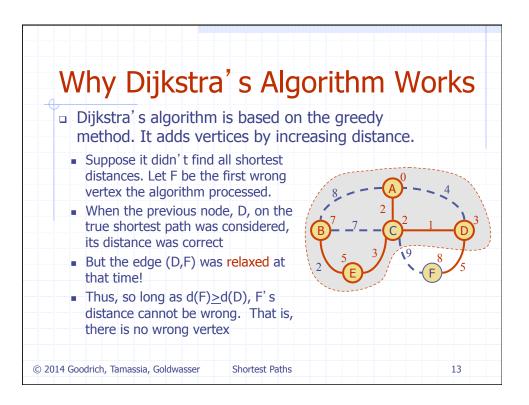


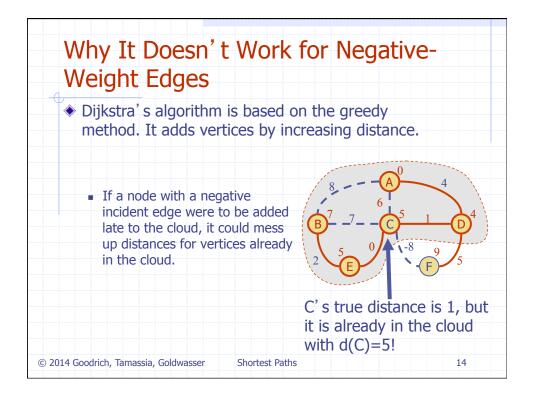


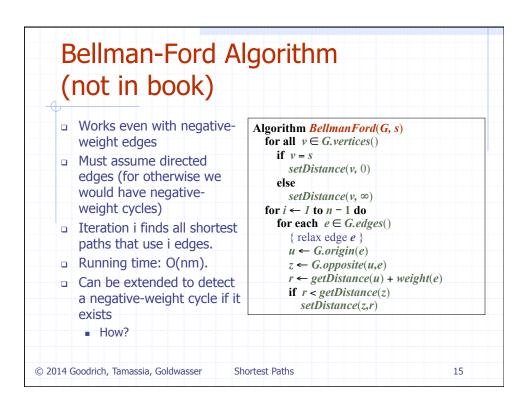


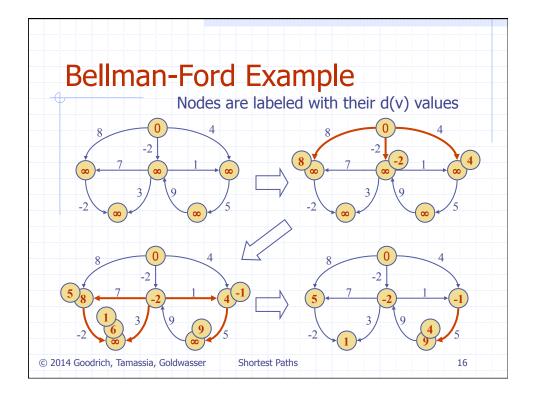
1	/** Computes shortest-path distances from src vertex to all reachable vertices of g. */	
$ \frac{2}{3}$	<pre>public static <v> Map<vertex<v>, Integer> shortestPathLengths(Graph<v,integer> g, Vertex<v> src) {</v></v,integer></vertex<v></v></pre>	
4	// d.get(v) is upper bound on distance from src to v	
5	Map <vertex<v>, Integer> $d = new$ ProbeHashMap<>();</vertex<v>	
6	// map reachable v to its d value	
7	Map < Vertex < V >, Integer> cloud = new ProbeHashMap <>();	
8	// pq will have vertices as elements, with d.get(v) as key	
9	AdaptablePriorityQueue <integer, vertex<v="">> pq;</integer,>	
10		
	pq = new HeapAdaptablePriorityQueue<>();	
	// maps from vertex to its pq locator	
11 12	// maps from vertex to its pq locator Map <vertex<v>, Entry<integer,vertex<v>>> pqTokens;</integer,vertex<v></vertex<v>	
11 12 13	// maps from vertex to its pq locator	
11 12	<pre>// maps from vertex to its pq locator Map<vertex<v>, Entry<integer,vertex<v>>> pqTokens; pqTokens = new ProbeHashMap<>();</integer,vertex<v></vertex<v></pre>	
11 12 13 14	<pre>// maps from vertex to its pq locator Map<vertex<v>, Entry<integer,vertex<v>>> pqTokens; pqTokens = new ProbeHashMap<>(); // for each vertex v of the graph, add an entry to the priority queue, with</integer,vertex<v></vertex<v></pre>	
11 12 13 14 15	<pre>// maps from vertex to its pq locator Map<vertex<v>, Entry<integer,vertex<v>>> pqTokens; pqTokens = new ProbeHashMap<>();</integer,vertex<v></vertex<v></pre>	
11 12 13 14 15 16	<pre>// maps from vertex to its pq locator Map<vertex<v>, Entry<integer,vertex<v>>> pqTokens; pqTokens = new ProbeHashMap<>(); // for each vertex v of the graph, add an entry to the priority queue, with // the source having distance 0 and all others having infinite distance for (Vertex<v> v : g.vertices()) { if (v == src)</v></integer,vertex<v></vertex<v></pre>	
11 12 13 14 15 16 17 18 19	<pre>// maps from vertex to its pq locator Map<vertex<v>, Entry<integer,vertex<v>>> pqTokens; pqTokens = new ProbeHashMap<>(); // for each vertex v of the graph, add an entry to the priority queue, with // the source having distance 0 and all others having infinite distance for (Vertex<v> v : g.vertices()) { if (v == src) d.put(v,0);</v></integer,vertex<v></vertex<v></pre>	
11 12 13 14 15 16 17 18 19 20	<pre>// maps from vertex to its pq locator Map<vertex<v>, Entry<integer,vertex<v>>> pqTokens; pqTokens = new ProbeHashMap<>(); // for each vertex v of the graph, add an entry to the priority queue, with // the source having distance 0 and all others having infinite distance for (Vertex<v> v : g.vertices()) { if (v == src) d.put(v,0); else</v></integer,vertex<v></vertex<v></pre>	
11 12 13 14 15 16 17 18 19	<pre>// maps from vertex to its pq locator Map<vertex<v>, Entry<integer,vertex<v>>> pqTokens; pqTokens = new ProbeHashMap<>(); // for each vertex v of the graph, add an entry to the priority queue, with // the source having distance 0 and all others having infinite distance for (Vertex<v> v : g.vertices()) { if (v == src) d.put(v,0);</v></integer,vertex<v></vertex<v></pre>	











Not in book) Works even with	Algorithm DagDistances(G, s) for all $v \in G.vertices()$ if $v = s$	
 negative-weight edges	setDistance(v, 0)	
Uses topological order Doesn't use any fancy	else setDistance (v, ∞)	
data structures	{ Perform a topological sort of the vertices }	
 Is much faster than Dijkstra' s algorithm	for $u \leftarrow 1$ to <i>n</i> do {in topological order} for each $e \in G.outEdges(u)$	
	$\{ \text{ relax edge } e \}$ $z \leftarrow G.opposite(u,e)$	
	$r \leftarrow getDistance(u) + weight(e)$ if $r < getDistance(z)$ setDistance(z,r)	

