











Partition Implementation Partition implementation Amortized analysis • A set is represented the Consider a series of k Partiton sequence of its elements ADT operations that includes A position stores a reference n makeSet operations back to the sequence itself (for Each time we move an operation *find*) element into a new sequence, • The position of an element in the size of its set at least the sequence serves as locator doubles for the element in the set An element is moved at most In operation *union*, we move log, *n* times the elements of the smaller sequence into to the larger Moving an element takes O(1) sequence time Worst-case running times The total time for the series ■ makeSet, find: O(1) of operations is $O(k + n \log n)$ • union: $O(\min(n_A, n_B))$

Campus Tour

© 2004 Goodrich, Tamassia

7

•	 Graph operations Methods <i>vertices</i> and edges are called once Method <i>endVertices</i> is called <i>m</i> times 	
*	Priority queue operations	
Ť	 We perform <i>m</i> insert operations and <i>m</i> removeMin operations 	erations
۲	Partition operations	
	 We perform <i>n</i> makeSet operations, 2m find operations more than n – 1 union operations 	and no
۲	Label operations	
	• We set vertex labels <i>n</i> times and get them 2 <i>m</i> times	
۲	Kruskal's algorithm runs in time $O((n + m) \log n)$ provided the graph has no parallel edges and is represented by the adjacency list structure	
	xdrich, Tamassia Campus Tour	8

Decorator Pattern Labels are commonly used in ۲ The decorator pattern extends the methods of the Position graph algorithms ADT to support the handling Auxiliary data of attributes (labels) Output has(a): tests whether the Examples position has attribute a DFS: unexplored/visited get(a): returns the value of attribute a label for vertices and unexplored/ forward/back set(a, x): sets to x the value of attribute a labels for edges destroy(a): removes attribute Diikstra and Prim-Jarnik: a and its associated value (for distance, locator, and cleanup purposes) parent labels for vertices The decorator pattern can be Kruskal: locator label for implemented by storing a vertices and MSF label for dictionary of (attribute, value) edges items at each position

Campus Tour

9

11

Traveling Salesperson Problem A tour of a graph is a spanning cycle (e.g., a cycle that goes through all

Campus Tour

- the vertices)
 A traveling salesperson tour of a weighted graph is a tour that is simple (i.e., no repeated vertices or edges) and has has minimum weight
- No polynomial-time algorithms are known for computing traveling salesperson tours
- The traveling salesperson problem (TSP) is a major open problem in computer science
 - Find a polynomial-time algorithm computing a traveling salesperson tour or prove that none exists

© 2004 Goodrich, Tamassia

Example of traveling salesperson tour (with weight 17)

10

TSP Approximation

- We can approximate a TSP tour with a tour of at most twice the weight for the case of Euclidean graphs
 - Vertices are points in the plane
 - Every pair of vertices is connected by an edge
 - The weight of an edge is the length of the segment joining the points
- Approximation algorithm
 - Compute a minimum spanning tree
 - Form an Eulerian circuit around the MST
 - Transform the circuit into a tour

© 2004 Goodrich, Tamassia