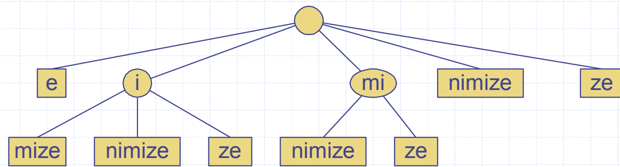
Tries

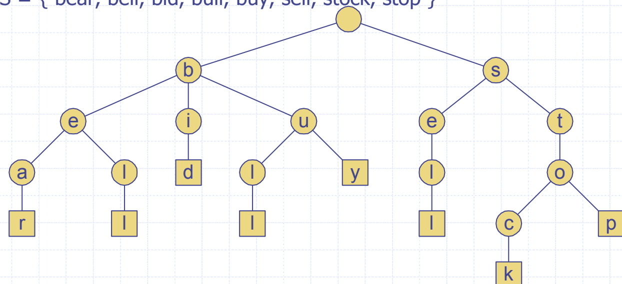


Preprocessing Strings

- Preprocessing the pattern speeds up pattern matching queries
  - After preprocessing the pattern, KMP's algorithm performs pattern matching in time proportional to the text size
- If the text is large, immutable and searched for often (e.g., works by Shakespeare), we may want to preprocess the text instead of the pattern
- A trie is a compact data structure for representing a set of strings, such as all the words in a text
  - A tries supports pattern matching queries in time proportional to the pattern size

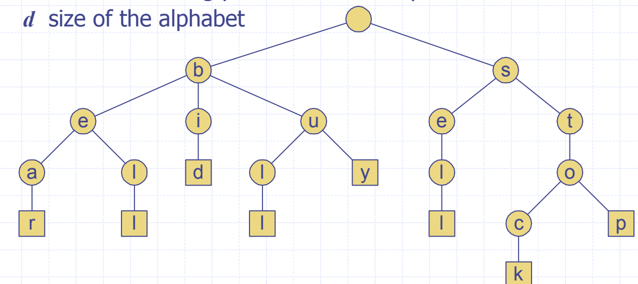
Standard Tries (§ 11.3.1)

- The standard trie for a set of strings S is an ordered tree such that:
  - Each node but the root is labeled with a character
  - The children of a node are alphabetically ordered
  - The paths from the external nodes to the root yield the strings of S
- Example: standard trie for the set of strings
  S = { bear, bell, bid, bull, buy, sell, stock, stop }



Analysis of Standard Tries

- A standard trie uses $O(n)$ space and supports searches, insertions and deletions in time $O(dm)$, where:
  - n total size of the strings in S
  - m size of the string parameter of the operation
  - d size of the alphabet



Word Matching with a Trie

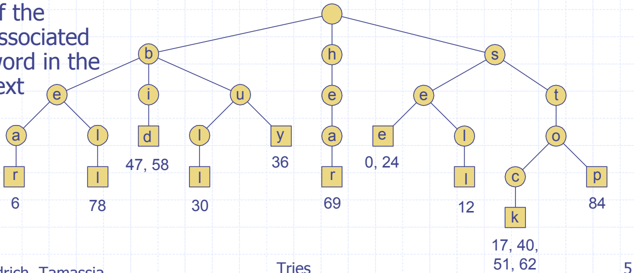
- We insert the words of the text into a trie
- Each leaf stores the occurrences of the associated word in the text

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
s	e	e		a		b	e	a	r	?		s	e	l	l		s	t	o	c	k	!	

24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46
s	e	e		a		b	u	l	l	?		b	u	y		s	t	o	c	k	!	

47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68
b	i	d		s	t	o	c	k	!		b	i	d		s	t	o	c	k	!	

69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88
h	e	a	r		t	h	e		b	e	l	l	?		s	t	o	p	!



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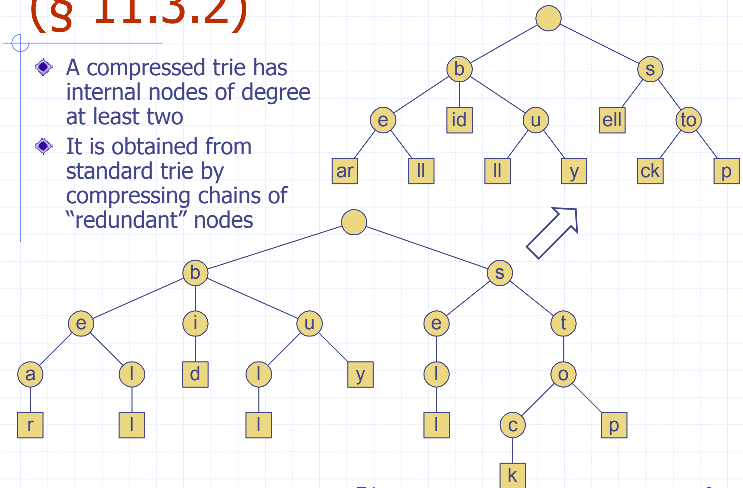
Compressed Tries (§ 11.3.2)

- A compressed trie has internal nodes of degree at least two
- It is obtained from standard trie by compressing chains of "redundant" nodes



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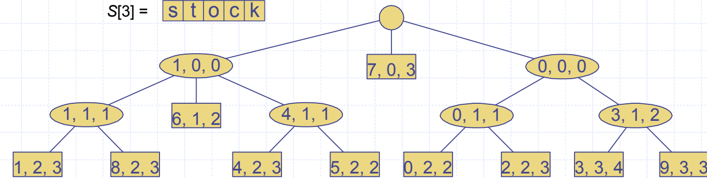
Compact Representation

- Compact representation of a compressed trie for an array of strings:
  - Stores at the nodes ranges of indices instead of substrings
  - Uses $O(s)$ space, where s is the number of strings in the array
  - Serves as an auxiliary index structure

	0	1	2	3	4
S[0] =	s	e	e		
S[1] =	b	e	a	r	
S[2] =	s	e	l	l	
S[3] =	s	t	o	c	k

	0	1	2	3
S[4] =	b	u	l	l
S[5] =	b	u	y	
S[6] =	b	i	d	

	0	1	2	3
S[7] =	h	e	a	r
S[8] =	b	e	l	l
S[9] =	s	t	o	p



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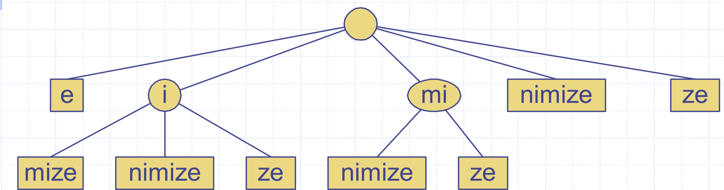
Suffix Trie (§ 11.3.3)

- The suffix trie of a string X is the compressed trie of all the suffixes of X

m	i	n	i	m	i	z	e
0	1	2	3	4	5	6	7



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Analysis of Suffix Tries

- Compact representation of the suffix trie for a string X of size n from an alphabet of size d
  - Uses $O(n)$ space
  - Supports arbitrary pattern matching queries in X in $O(dm)$ time, where m is the size of the pattern
  - Can be constructed in $O(n)$ time