

Recall Priority Queue Sorting (§ 7.1.4)

- We can use a priority queue to sort a set of comparable elements
 - Insert the elements with a series of insert operations
 - Remove the elements in sorted order with a series of removeMin operations
- The running time depends on the priority queue implementation:
 - Unsorted sequence gives selection-sort: O(n²) time
 - Sorted sequence gives insertion-sort: O(n²) time

Heaps

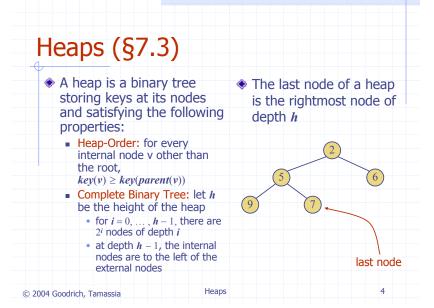


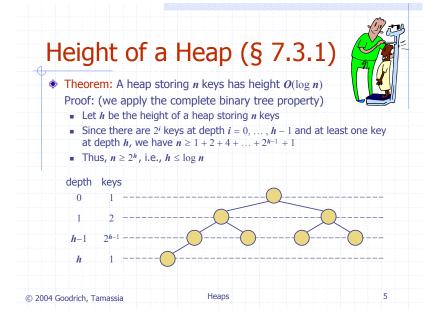


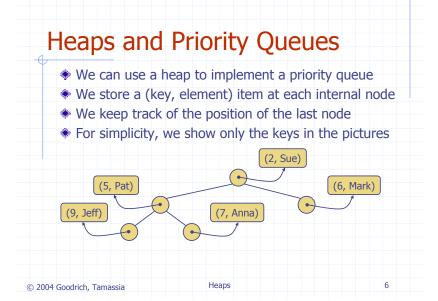
Algorithm *PQ-Sort***(S, C)**

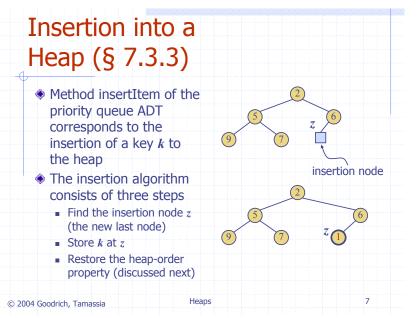
- Input sequence *S*, comparator *C* for the elements of *S* Output sequence *S* sorted in increasing order according to *C* $P \leftarrow$ priority queue with comparator *C* while $\neg S.isEmpty$ () $e \leftarrow S.remove$ (*S. first* ())
- $e \leftarrow S.remove (S. first ())$ P.insertItem(e, e)while $\neg P.isEmpty()$ $e \leftarrow P.removeMin()$ S.insertLast(e)

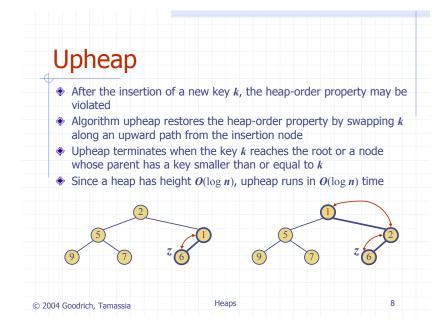
3

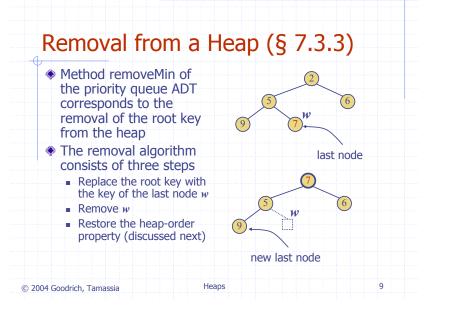


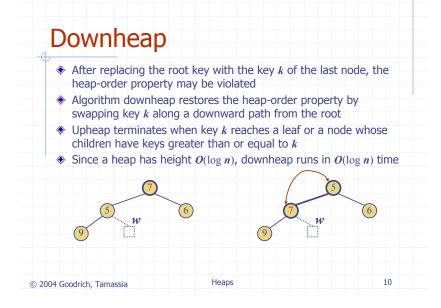


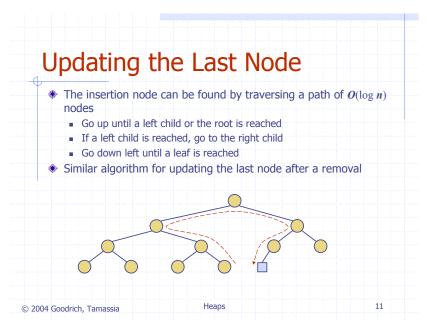


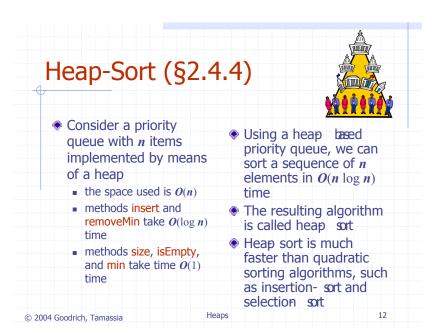


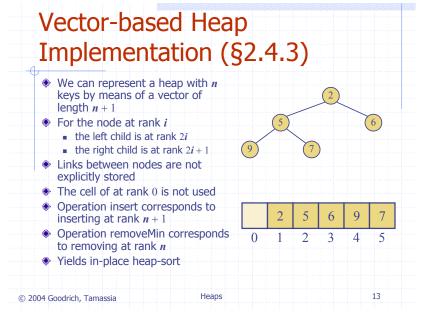


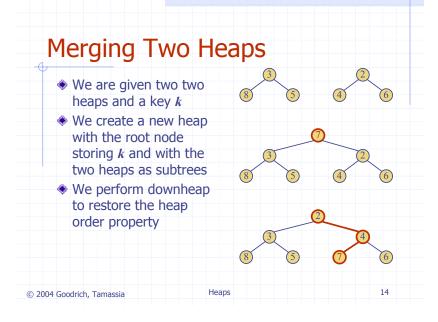












Bottom-up Heap Construction (§2.4.3) We can construct a heap storing *n* given keys in using a bottom up construction with log *n* phases • In phase *i*, pairs of heaps with $2^i - 1$ keys are merged into heaps with $2^{i+1}-1$ keys 2*i*+1_1 Heaps 15

